

National Qualifications 2022

2022 Applications of Mathematics

Higher

Finalised Marking Instructions

 $\ensuremath{\mathbb{C}}$ Scottish Qualifications Authority 2022

These marking instructions have been prepared by examination teams for use by SQA appointed markers when marking external course assessments.

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General marking principles for Higher Applications of Mathematics

Always apply these general principles. Use them in conjunction with the detailed marking instructions, which identify the key features required in candidates' responses.

For each question, the marking instructions are generally in two sections:

- generic scheme this indicates why each mark is awarded
- illustrative scheme this covers methods which are commonly seen throughout the marking

In general, you should use the illustrative scheme. Only use the generic scheme where a candidate has used a method not covered in the illustrative scheme.

- (a) Always use positive marking. This means candidates accumulate marks for the demonstration of relevant skills, knowledge and understanding; marks are not deducted for errors or omissions.
- (b) If you are uncertain how to assess a specific candidate response because it is not covered by the general marking principles or the detailed marking instructions, you must seek guidance from your team leader.
- (c) One mark is available for each •. There are no half marks.
- (d) If a candidate's response contains an error, all working subsequent to this error must still be marked. Only award marks if the level of difficulty in their working is similar to the level of difficulty in the illustrative scheme.
- (e) Only award full marks where the solution contains appropriate working. A correct answer with no working receives no mark, unless specifically mentioned in the marking instructions.
- (f) Candidates may use any mathematically correct method to answer questions, except in cases where a particular method is specified or excluded.
- (g) If an error is trivial, casual or insignificant, for example $6 \times 6 = 12$, candidates lose the opportunity to gain a mark, except for instances such as the second example in point (h) below.
- (h) If a candidate makes a transcription error (question paper to script or within script), they lose the opportunity to gain the next process mark, for example



The following example is an exception to the above



(i) Horizontal/vertical marking

If a question results in two pairs of solutions, apply the following technique, but only if indicated in the detailed marking instructions for the question.

Example:

Horizontal: ${}^{6}x = 2$ and x = -4 ${}^{6}y = 5$ y = -7Horizontal: ${}^{5}x = 2$ and x = -4 ${}^{6}y = 5$ and y = -7 ${}^{6}x = -4$ and y = 5 ${}^{6}x = -4$ and y = -7

You must choose whichever method benefits the candidate, **not** a combination of both.

(j) In final answers, candidates should simplify numerical values as far as possible unless specifically mentioned in the detailed marking instruction. For example

 $\frac{15}{12}$ must be simplified to $\frac{5}{4}$ or $1\frac{1}{4}$ $\frac{43}{1}$ must be simplified to 43 $\frac{15}{0.3}$ must be simplified to 50 $\frac{\frac{4}{5}}{3}$ must be simplified to $\frac{4}{15}$ $\sqrt{64}$ must be simplified to 8*

*The square root of perfect squares up to and including 144 must be known.

- (k) Commonly Observed Responses (COR) are shown in the marking instructions to help mark common and/or non-routine solutions. CORs may also be used as a guide when marking similar non-routine candidate responses.
- (I) Do not penalise candidates for any of the following, unless specifically mentioned in the detailed marking instructions:
 - working subsequent to a correct answer
 - correct working in the wrong part of a question
 - legitimate variations in numerical answers/algebraic expressions, for example angles in degrees rounded to nearest degree
 - omission of units
 - bad form (bad form only becomes bad form if subsequent working is correct), for example

 $(x^{3} + 2x^{2} + 3x + 2)(2x + 1)$ written as $(x^{3} + 2x^{2} + 3x + 2) \times 2x + 1$ $= 2x^{4} + 5x^{3} + 8x^{2} + 7x + 2$ gains full credit

- repeated error within a question, but not between questions or papers
- (m) In any 'Show that...' question, where candidates have to arrive at a required result, the last mark is not awarded as a follow-through from a previous error, unless specified in the detailed marking instructions.
- (n) You must check all working carefully, even where a fundamental misunderstanding is apparent early in a candidate's response. You may still be able to award marks later in the question so you must refer continually to the marking instructions. The appearance of the correct answer does not necessarily indicate that you can award all the available marks to a candidate.

- (o) You should mark legible scored-out working that has not been replaced. However, if the scored-out working has been replaced, you must only mark the replacement working.
- (p) If candidates make multiple attempts using the same strategy and do not identify their final answer, mark all attempts and award the lowest mark. If candidates try different valid strategies, apply the above rule to attempts within each strategy and then award the highest mark.

For example:

Strategy 1 attempt 1 is worth 3 marks.	Strategy 2 attempt 1 is worth 1 mark.
Strategy 1 attempt 2 is worth 4 marks.	Strategy 2 attempt 2 is worth 5 marks.
From the attempts using strategy 1, the resultant mark would be 3.	From the attempts using strategy 2, the resultant mark would be 1.

In this case, award 3 marks.

Marking Instructions for each question

Q	uestic	on	Generic scheme	Illustrative scheme	Max mark
1.			• ¹ Calculate monthly interest rate	• ¹ 0.72% stated or implied by • ²	3
			• ² Calculate loan outstanding at the end of month 1	• ² 5504.71	
			• ³ Calculate loan outstanding at the end of month 2	• ³ 5358.37	

Notes: 1.

Capital Interest Loan Time Repayment content of content of outstanding (months) (£) repayment repayment (£) (£) (£) 0 5650 1 186.01 40.72 145.29 5504.71 2 39.67 186.01 146.34 5358.37

2. At \bullet^1 , accept any answer which rounds to 0.7%.

3. If a candidate uses any incorrect interest rate mark 1 is not awarded but marks 2 and 3 may be awarded as follow through marks.

Commonly Observed Responses:

1. Based on candidate using 0.7% Award 3/3

Time (months)	Repayment (£)	Interest content of repayment (£)	Capital content of repayment (£)	Loan outstanding (£)
0				5650
1	186.01	39.55	146.46	5503.54
2	186.01	38.52	147.49	5356.05

2. Based on candidate using 0.72% Award 3/3

Time (months)	Repayment (£)	Interest content of repayment (£)	Capital content of repayment (£)	Loan outstanding (£)
0				5650
1	186.01	40.68	145.33	5504.67
2	186.01	39.63	146.38	5358.29

3. Based on candidate using (9/12) = 0.75% award 2/3

Time (months)	Repayment (£)	Interest content of repayment (£)	Capital content of repayment (£)	Loan outstanding (£)
0				5650
1	186.01	42.38	143.63	5506.37
2	186.01	41.30	144.71	5361.66

Q	uestic	on	Generic Scheme	Illustrative Scheme	Max Mark
2.	(a)		• ¹ Any six in correct sequence with	• ¹ see note 1	6
			durations	• ² see note 1	
			• ² Remaining 4 in correct sequence	• ³ see note 2	
			• ³ Forward scan A-E correct	• ⁴ see note 2	
			• ⁴ Forward scan for remaining 5		
			consistent with previous working	• ⁵ see note 3	
			• ⁵ Backward scan I,J,H,F and G		
			correct	• ⁶ see note 3	
			 ⁶ Backward scan for remaining 5 consistent with previous working 		



	Ques	tio	n		Generic Scheme												Il	lus	tra	ativ	/e	Sc	he	÷m	e				Max Mark							
2.	(b))		• ⁷ State number of days $•^7$ 4 days												1																				
 Notes: 1. Cannot have decimal days or part days or days and hours. 2. Answer must be based on the critical path if working is shown. 3. Answer based on 33 days leading to 4 days, award 0/1. 																																				
Commonly Observed Responses:																																				
	(c)	 •⁸ Add activities labels and plot activities A, B, and C •⁹ Interpret start times of D, E and I, J •¹⁰ Complete Gantt chart •¹⁰ See diagram note 1 											3																							
No	tes:																																			
1.		A						<u> </u>																												
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	ity	E			-			-										-																\square		_
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		_	1 2	2 3	4	5	6	7	8	9	10	11	12	13	14	15	1	6 17	18	8 19	20) 21	22	23	24	25	26	27	28	29	30	31	32	33	34 3	35
1. 2. 3.	All la but t Gant tasks Chec	ibe ask t c s/ti k f	ls m (s A (har me: or F	nust -Ji t n s. - in	t be mu nus <u>co</u>	e a st st orre	dd be be	ed cl cc	l to ea ons osi	o Ga rly isto tio	an la en n.	tt (be t ו	ch lle vit	art ed. ch	fo ei	or • the	• ⁸ ,	t nc	im o n e (e (h eec car	ou d fo ndi	rs) or da	the	et sP	ask PER	s a T (cha	s to art	o h	av r t	e t :he	:he • o	e la orig	be ina	lac alt	tivities: able of
Co	mmor	nly	Ob	ser	ve	d F	les	β	ons	ses	:																									

Q	uestic	n	Generic Scheme	Illustrative Scheme	Max Mark							
3.	(a)		• ¹ State type of data	• ¹ discrete numerical	1							
Note	es:											
1. Ac	1. Accept 'normally distributed', 'normal' or 'bell-shaped' at •1.											
Com	Commonly Observed Responses:											
	(b) • ² Valid explanation • ² eg a claim cannot be made from a graph OR one clinic in Edinburgh is not representative of the UK											
Note	es:			I								
1. S	tudy c	only co	ompleted over a one-year period (not r	elevant to location), award 0/1								
Com	monly	Obse	rved Responses:		1							
	(c)		• ³ State appropriate test	• ³ z-test for two proportions	1							
Note	es:			I								
1. A	chi-sq	uared	test is also appropriate for \bullet^3 .									
Com	monly	Obse	erved Responses:									
	(d)		• ⁴ State an appropriate design condition	• ⁴ eg samples need to be chosen randomly	1							
Note	es:											
Com 1. S	monly ample	Obse size	rved Responses: must be the same (not appropriate for	proportions) award 0/1								
	(e)		• ⁵ valid explanation	• ⁵ eg they are not comparable as the	1							
				data is not collected over the same time periods								
Note	s:											
 There must be comparison between months or seasons or time periods or temperature between the two clinics. •⁵ the seasonable variability could affect the results 												
Com	monly	Obse	erved Responses									
1. T	he tin	ne pei	riods/seasons must be the same (same	months), award 1/1								

Q	uestic	on	Generic Scheme	Illustrative Scheme	Max Mark
4.	(a)		Method 1	Method 1	3
			 ¹ Calculate balance on 1 January 2019 	• ¹ $(500 \times 1.033 + 500) = 1016.50$	
			• ² Calculate balance 1 January 2020	• ² $(1016.50 \times 1.024 + 500) = 1540.90$	
			• ³ Calculate balance at end of 2020	• ³ $(1540.90 \times 1.01) = 1556.30$	
			Method 2	Method 2	
			• ¹ Accumulate initial deposit	• ¹ $(500 \times 1.033 \times 1.024 \times 1.01) = 534.18$	
			• ² Accumulate second deposit	• ² $(500 \times 1.024 \times 1.01) = 517.12$	
			• ³ Accumulate third deposit and calculate balance at end of 2020	$ \begin{array}{r} \bullet^{3} & (500 \times 1.01 + 534.18 + 517.12) \\ &= 1556.30 \end{array} $	
Note 1. I 2. F	e s: f a cai availab final ai	ndidat Ie. nswer	e does not consider the additional £50 must be to 2 decimal places, ignore ar	00 each year then only mark 1 in meth	nod 2 is
Com	monly	0bse	erved Responses:	· •	
1. (2. (3. (500 x 500 x •³ acce	1.033 1.033 ept £1) + (500 x 1.024) + (500 x 1.01) = £1533 ³) + (500 x 1.024 ²) + (500 x 1.01), award 556.31(rounding) or £1556.29 (truncati	.50, award 0/3 1 0/3 on)	
	(b)		• ⁴ Calculate balance 1 January 2021	• ⁴ 1556.30 + 500 = \pounds 2056.30	2
			 ⁵ Calculate interest rate 	• ⁵ $\left(\left(\frac{2100}{2056.30}-1\right)\times100\right)=2.125\%$	
Note	s:				
1. ● 2 ⊑	⁴ still a	availa	ble following from \bullet^3	blo	
2. F 3. F	inal a	nswer	must be stated explicitly in percentag	e form	
Com	monly	0bse	erved Responses:		

Q	uestic	on	Generic Scheme	Illustrative Scheme	Max Mark				
5.	(a)	(i)	• ¹ Calculate appropriate school roll at end of year in cell D8	• ¹ eg =1-D7	3				
			• ² Use appropriate formula in C14	• ² eg =ROUND(\$D\$5*C8+\$D\$6,0)					
			³ Calculate school roll in August 2031 ⁴ Appropriate comment						
		(ii) • ⁴ Appropriate comment • ⁴ eg the number of pupils leaving each year is approximate							
1. • 2. • 3. • 4. F	¹ Can ² can ³ is or Roundi	be im be foi nly av ng no	plied by • ² (answer may not be in cell I und without the need for • ¹ eg =ROUND ailable for a whole number answer t needed, final answer will be 760, awa	D9) (C14(1-\$D\$8)+\$D\$10,0) ard 3/3					
Com 1 2 3 4 -	\bullet^1 a . \bullet^1 a . For = (! = (! = (! . •3 i . For - The - The	 Observation Observation Observation Observation Servation S	accept (C14+\$D\$10)-(C14*\$D\$8) cept the following with/without ROUNE C14+\$D\$10) C14+\$D\$10) C14+140) C14+140) Lable for following a pattern until Augu cept the following: ision of the prediction without rounding iction is not accurate as the number of) st 2031 g suggests decimal point pupils S1 pupils may change					
	(b)		• ⁵ Appropriate comment about roll	• ⁵ the school roll gradually increases each year	1				
Note 1. A 2. A	es: Accept Answer monly	posit must Obse	ive linear relationship be consistent with candidates working erved Responses:	in (a)					



Q	uestic	on	Generic Scheme	Illustrative Scheme	Max Mark
6.	(a)		• ¹ Calculate overall percentage	• ¹	1
			lincrease	$(((1.021 \times 1.005 \times 1.02) - 1) \times 100) = 4.66\%$	
Note 1. P	ercen	tage r	nust be explicitly stated ie 1.021 x 1.00	05 x 1.02 = 1.0466 award 0/1	
Com 1. 2 2. 2	monly 1 + 0 1 x 0	• Obse .5 + 2 .5 x 2	erved Responses: .0 = 4.6% award 0/1 .0 = 2.1% award 0/1		
	(b)		Method 1	Method 1	2
			 ² Calculate the price of petrol in 2018 	• ² $(136 \div 1.0466) = 130.3$	
			• ³ Calculate the cost of filling the tank	• ³ (45×1.303) = 58.64	
			Method 2	Method 2	
			• ² Calculate cost of tank in 2021	• ² $(1.364 \times 45) = 61.38$	
			• ³ Calculate the cost of filling the tank	• ³ (61.38 ÷ 1.0466) = 58.64	
Note	s:				
1. 2.	Acc Acc	ept 5 ept a	8.63, 58.65 nswers in pounds or pence		
Com 1. C	monly Candid ² and •	v Obse ates v	erved Responses: who correctly use 4.6% from (a) and get	t an answer of 130.4p leading to £58.68	3 award
2. •	³ can - 130 - 133	be aw).13 x 3.59 x	arded for a correct follow through fron 45 = 5855.85 45 = 6012	n an incorrect answer in \bullet^2 in method 1	



Q	uestic	on	Generic Scheme	Illustrative Scheme	Max Mark								
7.	(b)	(ii)	• ⁶ Generate coefficient and intercept	• ⁶ output from software (see below)	2								
			• ⁷ Communicate equation	• ⁷ jump height = $0.36 \times \text{back squat} + 7.2$									
Note	Notes:												
	Coefficients: (Intercept) Back 7.2366 0.3593												
Com	monly	v Obse	rved Responses:										
2	. For bac . For	a car ck squ y = 0	Ididate with the axes the wrong way r at = 1.9jump height + 7.2 .36x + 7.2 award 2/2 if both x and y a	round •' will be:									
	(c)		• ⁸ Generate estimate	• ⁸ output from software (see below) leading to an estimated vertical jump height of 66.5 cm	2								
			• ⁹ Appropriate comment	• ⁹ since 165kg is within the range of the data used to make the model and the model is a strong linear model									
				OR									
				the true value is likely to be between 56.7 and 76.3 cm									
Note	s:												
66.5	fit 2568	56.72	lwr upr 2259 76.32877										
1. V 2. E 3. ● 4. C	 With 66.5(cm) stated explicitly out-with the software output Estimate must be generated from a statistical output and not algebraically •⁹ is available for an appropriate comment based on previous working Comment using 'interpolation' in the context of the question, •⁹ can be awarded 												
Com 1.	Commonly Observed Responses: 1. Candidates that input 165 for jump leading to 351.954, •8 is not available												
	(d)		• ¹⁰ Appropriate comment	• ¹⁰ correlation is not causation	1								
Note	s:												
Com	monly	v Obse	erved Responses:										

Question		on	Generic Scheme	Illustrative Scheme	Max Mark
8.	(a)		• ¹ Calculate taxable income	• ¹ 3900 (per month) or 46 800 (per year)	3
			• ² Calculate taxable income for each band	• ² see table	
			• ³ Calculate tax for each band and total tax payable	• ³ see table (7667.67)	

Notes:

1. Table of taxable income and tax

Mark 2	2	Mark 3		
Taxable	Income	Tax Band	Tax	Payable
(£)			(£)	
12570		0%	0	
2097		1 9 %	398.4	3
10629		20%	2125.	80
18366		21%	3856.	86
3138		41%	1286.	58
		Total	7667.	67

- 2. For \bullet^2 taxable incomes must be stated
- 3. \bullet^2 can be awarded when taxable incomes are not stated but working is shown eg (14667-12570) x 0.19
- 4. \bullet^2 is awarded for correctly working out tax in each band and total

Commonly Observed Responses:

- 1. If \bullet^1 is not awarded then \bullet^2 and \bullet^3 can be awarded as follow through
 - 4000 (per month) or 48000 (per year) leading to 8159.67 award 2/3
 - 3640 (per month) or 43680 (per year) leading to 6388.47 award 2/3

Q	uestic	on	Generic Scheme	Illustrative Scheme	Max Mark	
8.	(b)		Method 1	Method 1	3	
			• ⁴ Calculate monthly pension contribution	•4 360		
			 ⁵ Calculate value of fund after second pension contribution 	• ⁵ $360 \times 1.1^{\frac{1}{12}} + 360 = 722.87$		
			• ⁶ Calculate value of fund after third pension contribution	$ \begin{pmatrix} \bullet^{6} \\ \left(722.87 \times 1.1^{\frac{1}{12}} + 360\right) = 1088.63 \end{cases} $		
			Method 2	Method 2		
			• ⁴ Accumulate initial pension payment	• ⁴ $\left(360 \times 1.1^{\frac{2}{12}}\right) = 365.76$		
			• ⁵ Accumulate second pension payment	• ⁵ $\left(360 \times 1.1^{\frac{1}{12}}\right) = 362.87$		
			• ⁶ Calculate value of fund after third pension contribution	• ⁶ $(365.76 + 362.87 + 360) = 1088.63$		
Note	Notes:					
Com 1. F	 Commonly Observed Responses: 1. For a monthly pension incorrectly calculated in •⁴, marks •⁵ and •⁶ can still be awarded: 100 leading to 304.81 award 2/3 260 leading to 786.24 award 2/3 					

Question		on	Generic Scheme	Illustrative Scheme	Max Mark			
8.	(c)		• ⁷ State reason	 ⁷ one reason from the following: It is important to save to provide an income in retirement when Sophie is not working. The employer's pension contribution is an extra part of the financial package which Sophie will not receive if she does not join the scheme. 	1			
Note	Notes:							
Com	Commonly Observed Responses:							

Question		on	Generic Scheme	Illustrative Scheme	Max Mark
9.	(a)		• ¹ Calculate monthly interest rate	• ¹ $(1.095)^{\frac{1}{12}} - 1 = 0.76\%$ per month	4
		• ² Create formula for interest, repayment and balance	 ² D16, E16, F16 (see spreadsheet) ³ check cells D63, E63 and F63 		
			 ³ Complete remainder of loan schedule for 48 months ⁴ Calculate monthly repayment, and adjust final repayment 	• ⁴ 374.06, 373.99	

Notes:

1. For marks $\bullet^1 \bullet^2$ and \bullet^3 see below

	Formula view	Numerical view
• ¹	(1+C8)^(1/12)-1	0.76%
• ²	D16= ROUND(F15*\$C\$9,2), E16=C16-D16, F16= F15-E16	D16=113.87, E16=260.19, F16=14739.81
• ³	D63= ROUND(F62*\$C\$9,2), E63=C63-D63, F63= F62-E63	D63=2.82 E63=371.17, F63= 0

2. If ROUND function has not been used \bullet^2 is not available

Commonly Observed Responses:

1. For an incorrect monthly interest rate, mark •1 is not available but follow through working to award marks 2, 3 and 4

- 0.79...% (9.5÷12) leading to 376.70 and 376.87 award 3/4

- 9.5% leading to 1443.52, 1439.05 award 3/4

Question		on	Generic Scheme	Illustrative Scheme	Max Mark
9.	(b)		 ⁵ Populate spreadsheet with payments £300pm plus £5000 in month 48 to buy car 	● ⁵ spreadsheet	3
			 ⁶ Set up formulae in in D16, E16, F136and copy down to use Goalseek to solve for monthly interest rate 	• ⁶ 0.87%	
			 ⁷ Calculate annual effective interest rate 	• ⁷ 11.04%	

Notes:

1. \bullet^6 and \bullet^7 may be solved in reverse order but need both to get correct answer.

2. Check cells C16 and C63 for \bullet^5

3. For	3. For •° see below						
	Formula view	Numerical view					
•6	D16= ROUND(F15*\$C\$9,2), E16=C16-D16, F16= F15-E16	D16=131.55, E16=168.45, F16=14831.55					

leading to 0.87...%

Commonly Observed Responses:

1. When 5000 is inserted in month 48 (cell C63), leading to 0.83% and 10.42% for marks 6 and 7 mark \bullet^5 is not available award 2/3

Question		on	Generic Scheme	Illustrative Scheme	Max Mark			
9.	(c)		• ⁸ State an appropriate reason	• ^{8.9} eg:	2			
			• ⁹ State a second appropriate reason	 Maria will own the car outright after 48 months without needing to find lump sum of £5000 The finance deal is risky- if Maria does not intend to keep the car but travels more than 24,000 miles she will pay more due to the penalty payment required The effective annual interest rate is higher on the finance deal if she does wish to keep the car. 				
Note	Notes:							
Com	Commonly Observed Responses:							

Q	uestic	on	Generic Scheme	Illustrative Scheme	Max Mark	
10.	(a)		 ¹ Find multiplying factor ² Calculate the population in 2032 and state conclusion 	• ¹ $\frac{1004}{680}$ • ² $\left(\text{eg } 1004 \times \frac{1004}{680} \right) \approx 1482$ The expert is incorrect since 1482 < 1600.	2	
Note 1. (2. • n Com	 Notes: (1600/680) x 1004 leading to 2032 and the expert is correct since 2032>1600 award ½ •² can only be awarded for relating a calculated answer to the expert's prediction, no need f numerical comparison Commonly Observed Responses: 					
	(b)		 ³ Estimate total amount of food eaten in adulthood ⁴ State assumption about maximum amount of termites and ants in diet ⁵ Estimate amount of termites and ants eaten based assumption 	 eg 30 kg × 365 days × 25 years = 273 750 kg eg assume 49% as a maximum percentage of diet (since mainly vegetarian). eg(49%×273 750)≈134 000 kg 	3	
Note 1.	 Notes: 1. Accept answers between 130 000 and 140 000 since the data in the question is given two significant figures. 					
Com 1. 2.	 Commonly Observed Responses: 1. •4 can only be awarded for assumptions between 49% - 49.9999% 2. •5 can be awarded for correctly using any percentage multiplied by their answer to •3 					

[END OF MARKING INSTRUCTIONS]