

X100/303

NATIONAL
QUALIFICATIONS
2002

MONDAY, 27 MAY
10.30 AM – 12.00 NOON

MATHEMATICS
HIGHER
Units 1, 2 and 3
Paper 2

Read Carefully

- 1 **Calculators may be used in this paper.**
- 2 Full credit will be given only where the solution contains appropriate working.
- 3 Answers obtained by readings from scale drawings will not receive any credit.



SCOTTISH
QUALIFICATIONS



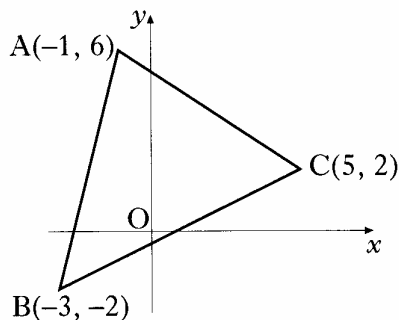
ALL questions should be attempted.

Marks

1. Triangle ABC has vertices A(-1, 6), B(-3, -2) and C(5, 2).

Find

- (a) the equation of the line p , the median from C of triangle ABC.
 (b) the equation of the line q , the perpendicular bisector of BC.
 (c) the coordinates of the point of intersection of the lines p and q .



3
4
1

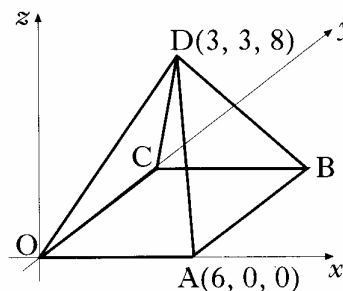
2. The diagram shows a square-based pyramid of height 8 units.

Square OABC has a side length of 6 units.

The coordinates of A and D are (6, 0, 0) and (3, 3, 8).

C lies on the y-axis.

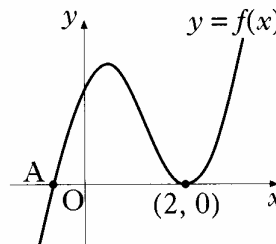
- (a) Write down the coordinates of B.
 (b) Determine the components of \vec{DA} and \vec{DB} .
 (c) Calculate the size of angle ADB.



1
2
4

3. The diagram shows part of the graph of the curve with equation $y = 2x^3 - 7x^2 + 4x + 4$.

- (a) Find the x -coordinate of the maximum turning point.
 (b) Factorise $2x^3 - 7x^2 + 4x + 4$.
 (c) State the coordinates of the point A and hence find the values of x for which $2x^3 - 7x^2 + 4x + 4 < 0$.

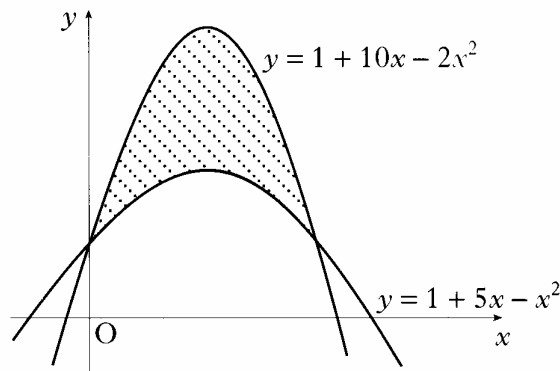


5
3
2

[Turn over

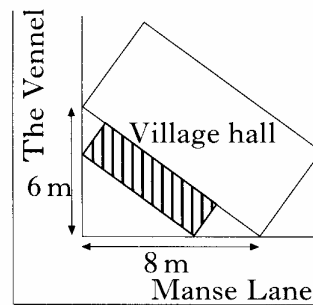
4. A man decides to plant a number of fast-growing trees as a boundary between his property and the property of his next door neighbour. He has been warned, however, by the local garden centre that, during any year, the trees are expected to increase in height by 0.5 metres. In response to this warning he decides to trim 20% off the height of the trees at the start of any year.
- (a) If he adopts the “20% pruning policy”, to what height will he expect the trees to grow in the long run? 3
- (b) His neighbour is concerned that the trees are growing at an alarming rate and wants assurances that the trees will grow no taller than 2 metres. What is the minimum percentage that the trees will need to be trimmed each year so as to meet this condition? 3

5. Calculate the shaded area enclosed between the parabolas with equations $y = 1 + 10x - 2x^2$ and $y = 1 + 5x - x^2$.

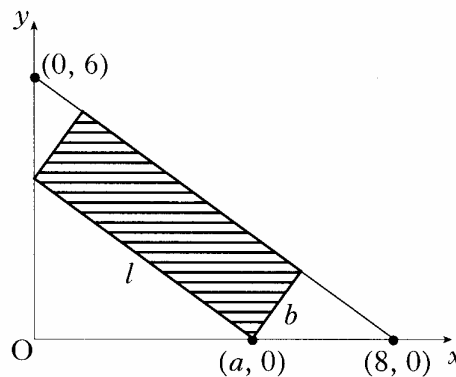


6. Find the equation of the tangent to the curve $y = 2\sin\left(x - \frac{\pi}{6}\right)$ at the point where $x = \frac{\pi}{3}$. 4
7. Find the x -coordinate of the point where the graph of the curve with equation $y = \log_3(x - 2) + 1$ intersects the x -axis. 3
8. A point moves in a straight line such that its acceleration a is given by $a = 2(4 - t)^{\frac{1}{2}}$, $0 \leq t \leq 4$. If it starts at rest, find an expression for the velocity v where $a = \frac{dv}{dt}$. 4
9. Show that the equation $(1 - 2k)x^2 - 5kx - 2k = 0$ has real roots for all integer values of k . 5

10. The shaded rectangle on this map represents the planned extension to the village hall. It is hoped to provide the largest possible area for the extension.



The coordinate diagram represents the right angled triangle of ground behind the hall. The extension has length l metres and breadth b metres, as shown. One corner of the extension is at the point $(a, 0)$.



- (a) (i) Show that $l = \frac{5}{4}a$.
- (ii) Express b in terms of a and hence deduce that the area, $A \text{ m}^2$, of the extension is given by $A = \frac{3}{4}a(8 - a)$. 3
- (b) Find the value of a which produces the largest area of the extension. 4

[END OF QUESTION PAPER]