



**X847/76/11**

**Mathematics  
Paper 1 (Non-calculator)**



Duration — 1 hour 15 minutes

**Total marks — 55**

**SECTION 1 — 44 marks**

Attempt ALL questions.

**SECTION 2 — 11 marks**

Attempt EITHER Part A OR Part B.

**You must NOT use a calculator.**

To earn full marks you must show your working in your answers.

State the units for your answer where appropriate.

You will not earn marks for answers obtained by readings from scale drawings.

Write your answers clearly in the spaces provided in the answer booklet. The size of the space provided for an answer is not an indication of how much to write. You do not need to use all the space.

Additional space for answers is provided at the end of the answer booklet. If you use this space you must clearly identify the question number you are attempting.

Use **blue** or **black** ink.

Before leaving the examination room you must give your answer booklet to the Invigilator; if you do not, you may lose all the marks for this paper.



\* X 8 4 7 7 6 1 1 \*

## FORMULAE LIST

### Circle

The equation  $x^2 + y^2 + 2gx + 2fy + c = 0$  represents a circle centre  $(-g, -f)$  and radius  $\sqrt{g^2 + f^2 - c}$ .

The equation  $(x - a)^2 + (y - b)^2 = r^2$  represents a circle centre  $(a, b)$  and radius  $r$ .

### Scalar product

$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}| |\mathbf{b}| \cos \theta$ , where  $\theta$  is the angle between  $\mathbf{a}$  and  $\mathbf{b}$

or  $\mathbf{a} \cdot \mathbf{b} = a_1 b_1 + a_2 b_2 + a_3 b_3$  where  $\mathbf{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}$  and  $\mathbf{b} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$ .

### Trigonometric formulae

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

$$= 2 \cos^2 A - 1$$

$$= 1 - 2 \sin^2 A$$

### Table of standard derivatives

$f(x)$	$f'(x)$
$\sin ax$	$a \cos ax$
$\cos ax$	$-a \sin ax$

### Table of standard integrals

$f(x)$	$\int f(x) dx$
$\sin ax$	$-\frac{1}{a} \cos ax + c$
$\cos ax$	$\frac{1}{a} \sin ax + c$

## SECTION 1 — 44 marks

Attempt ALL questions

1. Find the value of  $k$  for which the equation  $kx^2 + 3x - 4 = 0$  has equal roots. 3

2. Given that  $f(x) = (x^2 + 1)^5$ , find  $f'(1)$ . 3

3. A function  $f(x)$  is defined on  $\mathbb{R}$ , by

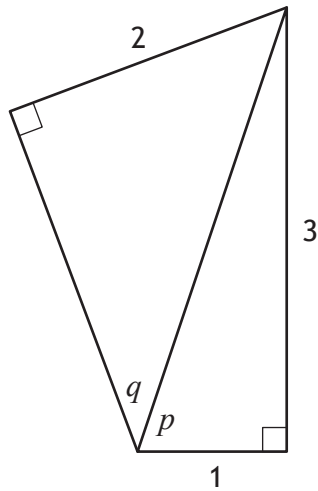
$$f(x) = \frac{x+3}{2}.$$

Find the inverse function,  $f^{-1}(x)$ . 3

4. Determine whether the line passing through  $(-4, 2)$  and  $(2, -7)$  is perpendicular to the line with equation  $3y = 2x + 9$ . 3

[Turn over

5. Two right-angled triangles are shown below.



(a) Determine the value of

(i)  $\sin p$

1

(ii)  $\cos q$ .

2

(b) Find the exact value of  $\cos(p + q)$ .

3

6. Functions  $f$  and  $g$  are defined on  $\mathbb{R}$  by

- $f(x) = 2x + 5$
- $g(x) = x^2 - 2x$ .

(a) Find an expression for  $f(g(x))$ .

2

(b) Find an expression for  $g(f(x))$ .

1

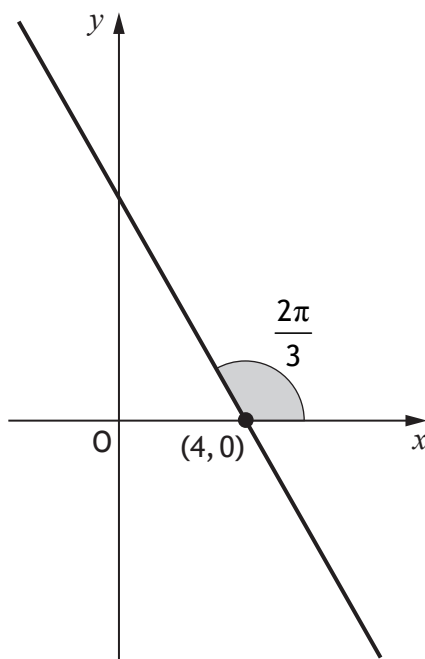
(c) Express  $g(f(x)) - f(g(x))$  in the form  $a(x + b)^2 + c$ .

4

7. Find  $\int 6 \cos\left(3x + \frac{\pi}{4}\right) dx$ .

8. A line makes an angle of  $\frac{2\pi}{3}$  with the positive direction of the  $x$ -axis.

It passes through the point  $(4, 0)$ .

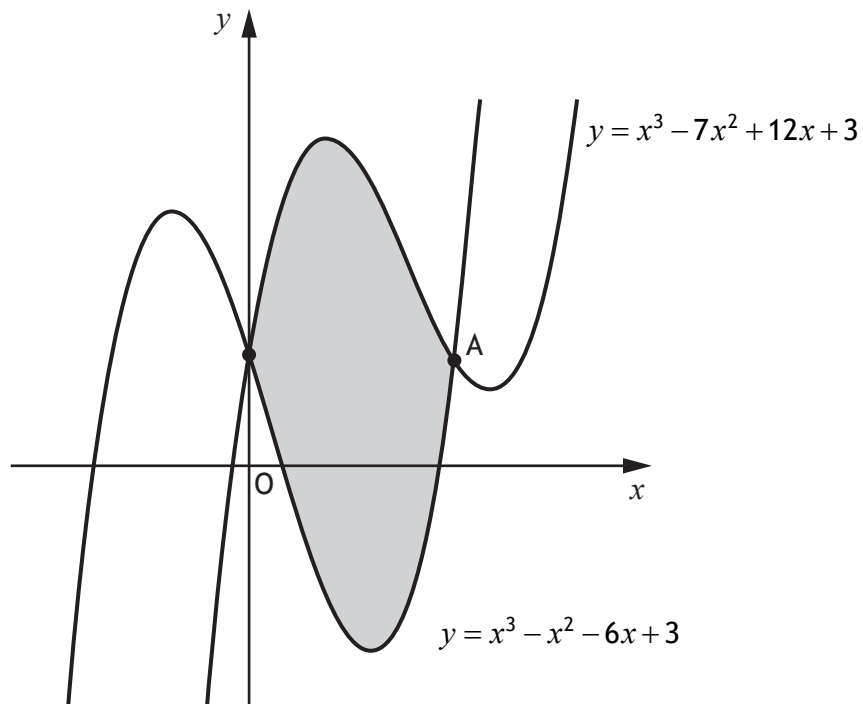


Determine the equation of the line.

[Turn over

9. The diagram shows the curves with equations  $y = x^3 - 7x^2 + 12x + 3$  and  $y = x^3 - x^2 - 6x + 3$ .

The curves intersect on the  $y$ -axis and at point A.



- (a) Find the  $x$ -coordinate of A. 2
- (b) Calculate the shaded area. 5
10. Factorise  $6x^3 - 13x^2 + 4$  fully. 4

11. A function,  $f$ , defined on  $\mathbb{R}$ , is such that

- the maximum value of  $f$  is 8
- the maximum occurs when  $x = 6$ .

The function  $g$  is given by  $g(x) = 2f(x) - 9$ .

(a) State the maximum value of  $g$ . 1

The function  $h$  is given by  $h(x) = f(x - 4) + 5$ .

(b) (i) State the maximum value of  $h$ . 1

(ii) State the value of  $x$  when the maximum value of  $h$  occurs. 1

[END OF SECTION 1]

[Turn over

SECTION 2 — 11 marks  
Attempt EITHER Part A OR Part B

Part A

12. Points A, B, and C are collinear, with B dividing AC.

- A has coordinates  $(4, 2, -5)$
- B has coordinates  $(7, -4, 1)$
- $|\vec{BC}| = 6$

- (a) (i) Find  $|\vec{AB}|$ . 2
- (ii) State the ratio in which B divides AC. 1
- (b) Determine the coordinates of C. 1

13. A sequence is generated by the recurrence relation  $u_{n+1} = \frac{2}{3}u_n + 8$ ,  $u_7 = 20$ .

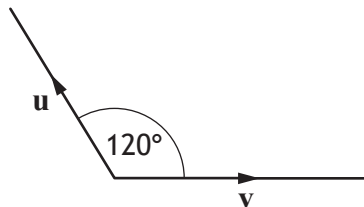
- (a) Determine the value of  $u_5$ . 2

This sequence approaches a limit as  $n \rightarrow \infty$ .

- (b) Determine the limit of this sequence. 2

14. The angle between vectors  $\mathbf{u}$  and  $\mathbf{v}$  is  $120^\circ$ .

$|\mathbf{u}| = 4$  and  $|\mathbf{v}| = 5$ .



Calculate  $\mathbf{u} \cdot (\mathbf{u} + \mathbf{v})$ .

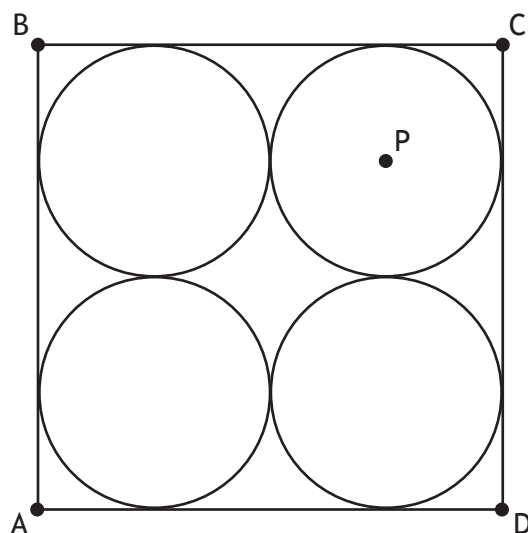
3



## Part B

15. ABCD is a square containing four congruent circles.

A is the point (2, 1), and D is the point (10, 1).

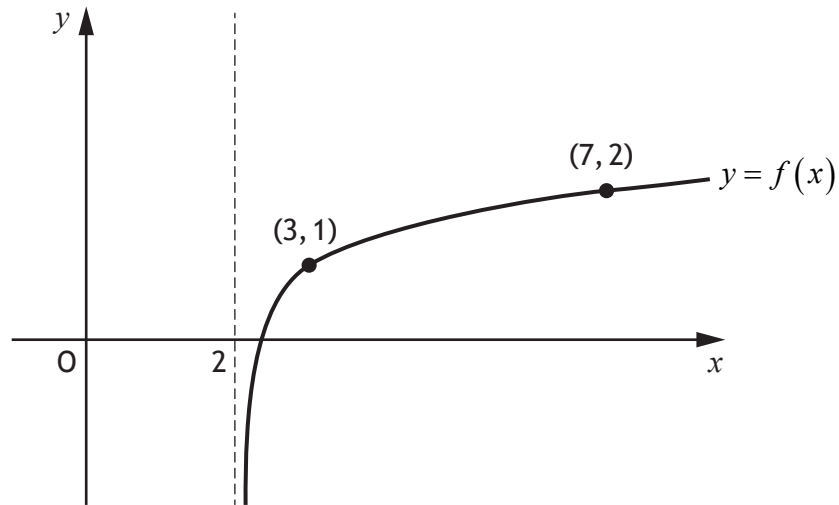


Determine the equation of the circle with centre P.

16. Evaluate  $\log_2 6 + \log_2 12 - 2\log_2 3$ .

[Turn over

17. A logarithmic function,  $f$ , is defined for  $x > 2$ .  
The diagram shows the graph of  $y = f(x)$ .



The inverse function,  $f^{-1}(x)$ , exists.

- (a) On the diagram in your answer booklet, sketch the graph of the inverse function. 2
- (b) Given that  $f(x) = \log_5(x - 2) + 1$ , find the coordinates of the point where the graph of  $f^{-1}(x)$  crosses the  $y$ -axis. 2

[END OF SECTION 2]

[END OF QUESTION PAPER]

[BLANK PAGE]

DO NOT WRITE ON THIS PAGE

[BLANK PAGE]

DO NOT WRITE ON THIS PAGE